



GB 2003 / 0 0 3 3 6 7



INVESTOR IN PEOPLE

The Patent Office
Concept House
Cardiff Road
Newport
South Wales
NP10 8QQ

REC'D 23 SEP 2003

WIPO PCT

PRIORITY DOCUMENT

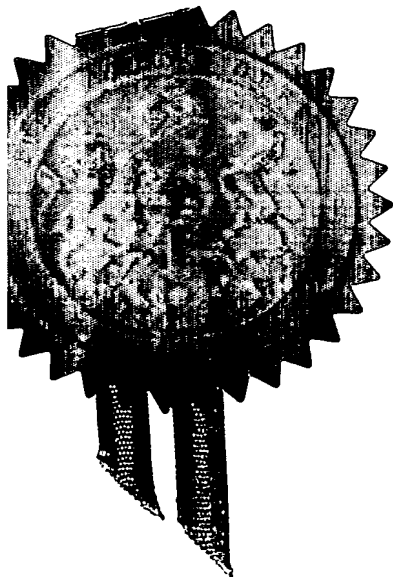
SUBMITTED OR TRANSMITTED IN
COMPLIANCE WITH RULE 17.1(a) OR (b)

I, the undersigned, being an officer duly authorised in accordance with Section 74(1) and (4) of the Deregulation & Contracting Out Act 1994, to sign and issue certificates on behalf of the Comptroller-General, hereby certify that annexed hereto is a true copy of the documents as originally filed in connection with the patent application identified therein.

In accordance with the Patents (Companies Re-registration) Rules 1982, if a company named in this certificate and any accompanying documents has re-registered under the Companies Act 1980 with the same name as that with which it was registered immediately before re-registration save for the substitution as, or inclusion as, the last part of the name of the words "public limited company" or their equivalents in Welsh, references to the name of the company in this certificate and any accompanying documents shall be treated as references to the name with which it is so re-registered.

In accordance with the rules, the words "public limited company" may be replaced by p.l.c., plc, P.L.C. or PLC.

Re-registration under the Companies Act does not constitute a new legal entity but merely subjects the company to certain additional company law rules.



Signed

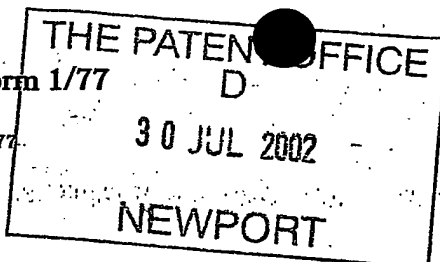
Dated

1 September 2003

BEST AVAILABLE COPY

Patents Form 1/77

Patents Act 1977
(Rule 16)



1777
30 JUL 02 0737062-3 000355
P01/7700 0:00-0217570.1

Request for grant of a patent

(See the notes on the back of this form. You can also get an explanatory leaflet from the Patent Office to help you fill in this form)

The Patent Office

Cardiff Road
Newport
South Wales
NP10 8QQ

1. Your reference W071555PGB
-
2. Patent application number 0217570.1
(The Patent Office will fill in this part) 30 JUL 2002
-
3. Full name, address and postcode of the or of each applicant (*underline all surnames*)
The University of Birmingham
Edgbaston
Birmingham
B15 2TT
- Patents ADP number (*if you know it*)
- If the applicant is a corporate body, give the country/state of its incorporation England 798165002
-
4. Title of the invention
METHOD AND APPARATUS FOR QUANTIFYING MATERIAL OR OBJECT PROPERTIES
-
5. Name of your agent (*if you have one*)
"Address for service" in the United Kingdom to which all correspondence should be sent (*including the postcode*)
Marks & Clerk
Alpha Tower
Suffolk Street Queensway
Birmingham, B1 1TT
England
- Patents ADP number (*if you know it*) 18002
-
- | | | | |
|---|---------|--|---|
| 6. If you are declaring priority from one or more earlier patent applications, give the country and the date of filing of the or of each of these earlier applications and (<i>if you know it</i>) the or each application number | Country | Priority application number
(<i>if you know it</i>) | Date of filing
(<i>day / month / year</i>) |
|---|---------|--|---|
-
- | | | |
|---|-------------------------------|---|
| 7. If this application is divided or otherwise derived from an earlier UK application, give the number and the filing date of the earlier application | Number of earlier application | Date of filing
(<i>day / month / year</i>) |
|---|-------------------------------|---|
-
8. Is a statement of inventorship and of right to grant of a patent required in support of this request? (*Answer 'Yes' if:*
a) any applicant named in part 3 is not an inventor, or
b) there is an inventor who is not named as an applicant, or
c) any named applicant is a corporate body.
See note (d)) YES

Patents Form 1/77

9. Enter the number of sheets for any of the -
following items you are filing with this form.
Do not count copies of the same document

Continuation sheets of this form

Description 23

Claim(s) 3

Abstract 1

Drawing(s) 6

10. If you are also filing any of the following,
state how many against each item.

Priority documents

Translations of priority documents

Statement of inventorship and right
to grant of a patent (Patents Form 7/77)

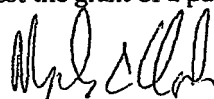
Request for preliminary examination
and search (Patents Form 9/77)

Request for substantive examination
(Patents Form 10/77)

Any other documents
(please specify)

11. I/We request the grant of a patent on the basis of this application.

Signature



Date

22/7/02

12. Name and daytime telephone number of
person to contact in the United Kingdom

D.I. WARD

0121 643 5881

Warning

After an application for a patent has been filed, the Comptroller of the Patent Office will consider whether publication or communication of the invention should be prohibited or restricted under Section 22 of the Patents Act 1977. You will be informed if it is necessary to prohibit or restrict your invention in this way. Furthermore, if you live in the United Kingdom, Section 23 of the Patents Act 1977 stops you from applying for a patent abroad without first getting written permission from the Patent Office unless an application has been filed at least 6 weeks beforehand in the United Kingdom for a patent for the same invention and either no direction prohibiting publication or communication has been given, or any such direction has been revoked.

Notes

- If you need help to fill in this form or you have any questions, please contact the Patent Office on 08459 500505.
- Write your answers in capital letters using black ink or you may type them.
- If there is not enough space for all the relevant details on any part of this form, please continue on a separate sheet of paper and write "see continuation sheet" in the relevant part(s). Any continuation sheet should be attached to this form.
- If you have answered 'Yes' Patents Form 7/77 will need to be filed.
- Once you have filled in the form you must remember to sign and date it.
- For details of the fee and ways to pay please contact the Patent Office.

Method and Apparatus for Quantifying Material or Object Properties

The present invention relates to a method and apparatus for quantifying material properties. More particularly, the invention relates to such methods and apparatus which rely upon a spectral analysis of light remitted, emitted, and/or transmitted from the material or object under test.

There are many situations in which non-invasive and non-destructive methods of analysing an object or material are desirable or even necessary. For example, in the medical field, it is often desirable to be able to analyse the properties of tissue *in vivo*, avoiding the need for biopsies and other invasive and destructive techniques. One technique employed for this purpose relies upon an analysis of light reflected (or more correctly "remitted") by an area of tissue. Assuming that the illuminating light penetrates the tissue to some depth and is reflected (or scattered or/and absorbed) to different degrees at different depths, an analysis of the remitted light can provide useful information about the properties of the tissue.

Techniques such as that described in the preceding paragraph build upon so-called "physics-based" approaches to computer vision. In contrast to traditional image analysis techniques which analyse a final image, physics-based approaches rely on a fundamental understanding of the image formation process. This process consists of an involved series of interactions of the illuminating light at, and within, object surfaces. By using an understanding of these interactions, relationships between scene parameters and image values are established. Physics-based approaches have been shown to be successful in many different areas of image understanding, such as obtaining shape from shading, and removing the effects of variations in illumination prior to image segmentation.

A technique for non-invasively analysing skin structure is described in International patent application publication number WO98/22023. This technique uses a physics-based computer vision approach. The technique described in this publication makes use of a calibration step in order to take into account the fact that the skin illumination conditions may vary from one measurement to the next. The calibration step requires

the use of some additional equipment and also adds to the overall analysis time. Whilst this may not present a problem for analysing skin, it may present a problem for analysing other body tissues. For example, it may not be possible to provide additional calibration components on probes used for internal examination (such as endoscopes), whilst calibration is difficult to achieve when analysing the fundus of the eye due to the complexity of the eye structure and the unpredictability of the intervening lens. It will be appreciated that calibration may also present problems when analysing non-body materials where proximity or contact of the calibration medium with the material analysed is difficult or impossible.

Substantial work has been carried out to develop image analysis algorithms which are able to identify different objects irrespective of the illuminating light. Many of the techniques developed are based around the linear model of surface reflectance as proposed in L. Maloney and B. Wandell, "Color constancy: a method for recovering surface spectral reflectance", J. Opt. Soc. Am. A 3, 29-33 (1986). This approach is based on the idea that the surface reflectance of any object within an imaged scene can be expressed as a weighted sum of basis spectral reflectance functions:

$$S(\lambda) = \sum_{j=1}^n \sigma_j S_j(\lambda) \quad (1)$$

and that the illuminating light can similarly be expressed as a weighted sum of basis lights. It has been shown that only a small number of basis functions are required to obtain accurate approximations to the surface reflectances of many naturally occurring objects and also the spectral variation of natural daylight.

With this technique it is possible to recover the vector of weighting constants σ_j from a vector of image values and thus specify the spectral reflectance of the imaged object at every pixel. Every potential imaged object/object characteristic will have a unique spectral reflectance. Thus, if the spectral reflectance can be determined using a linear model, then the parameter vector can be specified. With this approach it should be possible to recover a parameter vector from the vector of image values at each pixel. Unfortunately the method is only able to recover the weighting constants σ_j to within a multiplicative scaling factor and thus cannot be used to specify the exact spectral reflectance and therefore the exact parameter vector.

An approach to geometry-insensitive segmentation of images has been developed in G. Healey, "Using colour for geometry-insensitive segmentation," J. Opt. Soc. Am. A 6, 920-937 (1989), and is based on the idea of normalised colour. With this approach image values are first divided by an estimate of normalised colour. This estimate is based on approximating the incoming signal from colour pixel values by using a finite-dimensional linear approximation to represent the colour signal. Using these normalised values, different metal and dielectric materials can be identified across an imaged scene in which the geometry varies considerably.

A similar technique has been applied to evaluate burn injuries {M. A. Afromowitz, G. S. van Liew and D. M. Heimbach, "Clinical evaluation of burn injuries using an optical reflectance technique", IEEE trans. Biomed. Eng. BME-34, 114-127 (1987), and M. A. Afromowitz, J. B. Callis D. M. Heimbach, L. A. Desoto and M. K. Norton, "Mulitspectral imaging of burn wounds: a new clinical instrument for evaluating burn depth", IEEE tran. Biomed. Eng. 35, 842-849 (1988)}. In this case, RGB image values were normalised by dividing them by the response of an IR filter. From the normalised values it was possible to assess the extent of burn damage across a given area of imaged skin.

There exists a need for a non-invasive technique for analysing an object or material (which may be complex, for example multi-component and/or multi-layer and which may be solid, gaseous, liquid, etc) which does not require calibration to take into account changing illumination conditions. It is an object of the present invention to provide such a technique. This and other objects are achieved by designing optimal spectral filters which will select light components which can be mapped uniquely to the object/material properties of interest, with a sufficiently high resolution.

According to a first aspect of the present invention there is provided a method of determining a property or properties of each of a set of filters, which filters are used to select specific wavelength ranges in a system which relies upon a spectral analysis of remitted, emitted, and/or transmitted light to quantify a parameter or parameters of an object or material, the method comprising the steps of:

- 1) defining a set of potential filter properties
- 2) defining one or more image quotients, the or each image quotient for a region being obtained by dividing the quantified output of a given filter for that region, the "image value" for that filter, by another image value for that same region;
- 3) for an object or material to be analysed and for said defined set of potential filter properties and for said given image quotients, obtaining a function mapping points in parameter space to points in image quotient space;
- 4) determining whether the mapping function provides a 1:1 correspondence between points in parameter space and points in image quotient space; and
- 5) if the mapping function does not provide a 1:1 correspondence, rejecting said potential filter properties, repeating steps 1) to 4) and, if the mapping function does provide a 1:1 correspondence accepting the potential filter properties as a candidate set of filter properties.

The key step in the present invention is that of identifying a set of filter properties and image quotients and a mapping function which maps image quotients to object/material parameters with a 1:1 correspondence. This first step may require consideration of many potential filter properties and corresponding mapping functions.

Preferably, for each filter the method of the present invention is used to determine the centre wavelength of the filter. The method may additionally be used to determine the full width half maximum (FWHM) of the filter characteristic.

Preferably, step 3) comprises constructing a Jacobian matrix for the mapping function with respect to said parameter(s), and obtaining the determinant of that matrix. If the determinant is strictly positive or strictly negative over the entire parameter space, then a 1:1 correspondence between points in parameter space and points in image quotient space is assumed. It will be appreciated that these operations may be performed using multiple processing steps or may be combined into a single processing step.

Embodiments of the present invention may involve the calculation of an error, indicative of the accuracy of parameter recovery obtained using said mapping function. The error may be calculated as follows:

- a) calculate the error associated with image acquisition for each vector of each image quotient;
- b) from the image quotient vector error, calculate the maximum possible error in each component of the parameter vector across the whole of parameter space; and
- c) use the vector of parameter errors at each point within parameter space to measure the accuracy of parameter recovery.

The present invention may be incorporated into many different filter property calculation schemes. For example, in a scheme using a genetic algorithm, the method may be used to identify a plurality of candidate filter parameter sets. The method of the present invention is then applied repeatedly to find an optimal filter parameter set using the candidates. Alternatively, the method may be employed in a scheme using a gradient descent algorithm. In such a scheme, the method of the present invention is employed to identify a first candidate set of filter parameters. This set is then used to make a selection of another set of filter properties, and the process repeated as often as necessary to arrive at an optimal solution. Of course, any suitable optimization algorithm can be used to compute an optimal solution or a solution which has sufficient accuracy.

The present invention may be employed in many different technical fields. However, one field in which it is particularly applicable is that of medical diagnosis and testing, for example analysing skin structure.

Each time the method steps 1) to 4) are carried out, the image quotients may or may not be changed. That is to say that, for each repetition, the potential filter properties and the image quotients may be changed, or only the potential filter properties may be changed.

According to a second aspect of the present invention there is provided apparatus for analysing an object or material having means for conducting a spectral analysis of remitted, emitted, and/or transmitted light to quantify a parameter or parameters of an object or material, the apparatus comprising a plurality of filters for splitting said light

into respective components, the filters having properties obtained by using the method of the above first aspect of the invention.

It will be appreciated that the filters of the apparatus may be implemented in optical, electrical/electronic, or software form.

For a better understanding of the present invention and in order to show how the same may be carried into effect, reference will now be made by way of example to the accompanying drawings, in which:

Figure 1 illustrates a function f which maps an image quotient \bar{i} to a material parameter P ;

Figure 2 illustrates a combination of errors in parameter space, mapped to image quotient vector space;

Figure 3 illustrates a model of the layered structure of skin;

Figures 4a and 4b show how the reemitted spectrum (intensity vs wavelength) varies for different melanin and blood levels respectively;

Figure 5 illustrates a set of filters suitable for analysing blood and melanin levels in skin; and

Figure 6 is a flow diagram illustrating a method of defining a set of filter properties for use in analysing the properties of an object or material.

Most physics-based approaches used in computer vision employ what is known as the dichromatic model. A detailed explanation of this model is given in S.A. Shafer, "Using colour to separate reflection components," Col. Res. Appl. 10, 210-218 (1985). The dichromatic model states that light remitted from an object is the sum of two components, a "body" component and a "surface" component. The body component relates to physical processes occurring after penetration of light into the material and the surface component relates to reflections which take place at the surface of the object. The body component is a function of the spectral characteristics of the object, whereas the surface component depends only on the object geometry and the incident light. The model states further that each component can be considered as the product of a geometrical term and a wavelength dependent term.

In a typical analysis system, light remitted from an object can be measured using a digital camera with a small number of optical filters. Image values - brightness or "intensity" - for each image location (x, y) for a given filter (the n th filter) are given by:

$$\begin{aligned} i^n(x, y) &= K_b C_b^n + K_s C_s^n \\ &= K_b \int E(\lambda) S(\lambda) R^n(\lambda) d\lambda + K_s \int E(\lambda) R^n(\lambda) d\lambda \end{aligned} \quad (2)$$

where K_b and K_s are the geometric terms of the body and surface components respectively and C_b^n and C_s^n are colour terms. The first integral in equation (2) is the product of three terms: $E(\lambda)$ is the illuminating light, $S(\lambda)$ is the spectral remittance from the body of the imaged object, and $R^n(\lambda)$ is the spectral response of the n th optical filter. In the second integral there are only two terms as there is no wavelength dependence on the surface component of reflection. The dichromatic reflection model is very important for 3-D scene analysis as it allows for both colour and geometrical analysis of objects within a scene.

The approach presented here is concerned with problems in which the surface term in equation (2) can be neglected. Although this would appear to limit the class of problems to scenes containing objects which do not have a specular component of reflection, such as many organic objects, image processing algorithms have been developed to allow removal of this component of reflection giving greater applicability of the technique. For example, it has been shown that it is possible to remove the highlights from complex images containing inhomogeneous dielectrics. It is also possible to remove the surface component of reflection using a polarising filter. Once this component has been removed from image data, it will be possible to use the techniques described here.

A key issue is to show that the technique proposed here is valid for problems where the intensity of the illuminating light is unknown (whilst assuming that the spectral definition of the illuminating light is known). For this purpose the incident light is written as:

$$E(\lambda) = \epsilon_0 E_0(\lambda) \quad (3)$$

where ϵ_0 is a wavelength independent scaling factor. Equation (2) now becomes

$$i^n(x, y) = \epsilon \int E_0(\lambda) S(\lambda) R^n(\lambda) d\lambda \quad (4)$$

where $\epsilon = \epsilon_0 K_b$. A digital camera records an N -dimensional vector of image values at each location $(x; y)$. If a mapping, which is independent of the constant ϵ , can be established between the vector of image values and the vector of parameters, then it will be possible to recover scene parameters from image data in a way that does not depend on illumination intensity or scene geometry.

We now introduce the concept of an image quotient, obtained by dividing one image value, calculated from equation (4), by another. For a given image vector, the n th image quotient is given as:

$$\bar{i}^n = \frac{i^n}{i^m} \quad n \neq m. \quad (5)$$

Simple consideration of equation (4) shows that any quotient defined in this way will be invariant to a change in the parameter ϵ . Thus any method for the recovery of parameter values from image quotients will be independent of scene geometry and illumination intensity.

The approach presented here is fundamentally different from most other work related to colour constancy. The goal in earlier work was to remove the effects of geometry and illumination prior to either segmentation or pixel or object classification. Both of these tasks require that pixels belonging to a particular class or object are statistically similar. The operations to remove the dependency on geometry and illuminating light change colour representation such that pixels are now clustered on the basis of the similarity of their intrinsic surface colouration. In contrast, the objective here is to extract quantitative parameters upon which the object colouration depends, not to find statistical similarities. Moreover, the specific filters are chosen to maximise the distance in the image quotient space between vectors corresponding to similar parameter values, as this minimises the error on the parameter value recovered from the colour image.

The technique described is generally applicable to scenes in which a small number of parameters are required to describe all possible objects/object characteristics. In the

formulation, the parameters will be considered to vary continuously. Thus, the technique will be particularly applicable to problems where object characteristics need to be measured across an image. For example a medical imaging system may be required to analyse a particular tissue. The underlying structure of the tissue will not vary, only specific characteristics such as thickness of the different layers (including zero thickness) or the concentration of a particular chemical constituents (including zero concentration). In this situation a small parameter vector can describe all possible variations in the characteristics of the imaged scene. For K scene parameters the parameter vector is defined as:

$$\mathbf{p} = \sum_{k=1}^K p_k \quad \mathbf{p} \in \mathbf{P} \quad (6)$$

and the space \mathbf{P} defines all potential object characteristics. Ultimately, a mapping from image quotients back to the parameter vector is required, but first the forward problem of obtaining image quotients for a given parameter vector is considered. A reflectance spectrum, corresponding to a given point within parameter space, can be described by the vector in M dimensional wavelength space:

$$\lambda = \sum_{m=1}^M \lambda_m \quad \lambda \in \Lambda \quad (7)$$

where the space Λ defines all possible spectral reflectance functions. The mapping a , defined as

$$a : \mathbf{P} \longrightarrow \Lambda \quad (8)$$

is introduced to denote the mapping from parameter space to wavelength space. This mapping gives the spectral reflectance of the object specified by the vector \mathbf{p} . Such a mapping can be achieved either by a spectroscopic measurement, or by using a mathematical model which takes as input the parameters and produces a corresponding reflectance spectrum. Models of light propagation in different media, such as the Monte Carlo method or the Kubelka Munk approximation, can be used for this purpose. It must be possible to perform this mapping across the whole of parameter space, thus defining every possible spectral reflectance function.

A digital camera with N optical filters records an N -dimensional image vector at each pixel. The image vector is given as:

$$\mathbf{i} = \sum_{n=1}^N i^n \quad \mathbf{i} \in \mathbf{I} \quad (9)$$

where \mathbf{I} describes the space of all possible image values. The process of image acquisition can be considered as the projection of points in wavelength space to points in filter space. This projection is performed by the mapping function:

$$b : \Lambda \longrightarrow \mathbf{I}. \quad (10)$$

Equation (4) performs this mapping b in continuous form. In discrete form, the response of the n th optical filter, is given as:

$$i^n = \epsilon \sum_{m=1}^M R_m^n \lambda_m \quad (11)$$

where $\lambda_m = E_0(\lambda)S(\lambda)$ and the positive weights at each wavelength are given by R_m^n , thus defining each filter response function. A digital camera effectively performs the mapping b , projecting points from a large dimensional space (wavelength space) to a small dimensional space (filter space). With such a mapping there will be a substantial loss of information. However, even with this loss of information, it should be possible to define the mapping in such a way that accurate information regarding the original parameter values can still be recovered from image data. Conditions for this mapping will be discussed in the following later.

Most current image acquisition systems use an RGB system of filters. Although this defines a potential mapping b , it may not be the best mapping with which to recover parameter values from image data. However, it is known to select specific filters to obtain better clarity of data than that possible with an RGB system (although mainly for visualization or image segmentation, not for quantification). Also, in spectrometry, particular spectral wavelengths are selected using statistical methods to improve quantification of components in mixtures. It will therefore be appreciated that an objectively defined set of optical filters is able to perform the task of recovery of parameters, which describe the variation in human skin, better than a standard RGB system.

Once the vector of image values has been obtained, a vector of image quotients can be

calculated using equation (5). The vector of image quotients is given as:

$$\bar{i} = \sum_{n=1}^{\bar{N}} \bar{i}^n \quad \bar{i} \in \bar{I} \quad (12)$$

where \bar{I} describes the space of all possible image quotients. The mapping from filter space to the space of image quotients is performed after image acquisition and will be referred to as mapping c , defined as:

$$c : I \longrightarrow \bar{I}. \quad (13)$$

There are many ways to define the image quotients and thus the mapping c . For example, pairs of image values could be used to define image quotients as:

$$\bar{i}^n = \frac{i_{2n-1}}{i_{2n}} \quad n = 1, 2, \dots, \frac{N}{2} \quad (14)$$

or a single image value could be taken as the denominator with which to calculate image quotients from the remaining image values, for example:

$$\bar{i}^n = \frac{i_n}{i_1} \quad n = 2, 3, \dots, N. \quad (15)$$

At most the dimensionality, \bar{N} , of the new space will be one less than that of the original filter space, N . This would correspond to the definition given in equation (15). Alternatively, if the image quotients were defined as given in equation (14), then the dimensionality of the new space will be half that of the original filter space. The aim is to recover a K -dimensional parameter vector from \bar{N} image quotients. Thus there must be at least as many image quotients as parameters, that is, $\bar{N} \geq K$.

The function f defined as:

$$f = a \circ b \circ c \quad f : P \longrightarrow \bar{I} \quad (16)$$

represents the three stage mapping from parameter space to wavelength space, to image space, and finally to the space of image quotients. For a given set of optical filters, it will be possible to perform this mapping across the whole of parameter space, provided that it is possible to obtain a spectrum for any given parameter vector. The inverse of function f is defined as:

$$f^{-1} : \bar{I} \rightarrow P$$

(17)

and maps from the space of image quotients directly to parameter space. If it is possible to define an appropriate f^{-1} , it will be possible to recover parameter values from image data in a way that is independent of illumination intensity and scene geometry. The ultimate aim is to find the optimum f^{-1} which maximises the accuracy of parameter recovery. Before a detailed discussion of this mapping is presented, it is important to emphasise that the form of the function f will depend on the mappings a , b and c . Although mapping a is fixed for a given problem, mapping b will vary with the choice of optical filters and mapping c will vary depending on how the image quotients are defined.

Any mapping function which is to map from the space of image quotients (\bar{I} -space) to parameter space (P -space) must be 1 to 1. That is, for a given point in P -space, there must be a corresponding unique point in \bar{I} -space and *vice-versa*. If this is not the case, ambiguity will arise as it could be possible to recover more than one set of parameter values from a given vector of image quotients. Once this condition has been established, it is necessary to consider the error associated with parameter recovery as, using a digital camera, it will only be possible to obtain image values to within a given uncertainty. This will introduce an uncertainty into the final recovery of the parameter vector. There could also be an error associated with the prediction/measurement of a spectrum from the parameter vector. For simplicity the analysis presented here will be restricted to problems in which the error associated with the spectral measurement can be neglected.

Initially, the problem where one parameter is sufficient to describe all variation in an imaged scene will be analysed. The methodology will then be extended to problems where the number of parameters is greater than one.

Consider the case where one image quotient (two image values) is used to recover a single parameter value. Figure 1 illustrates a function f which gives the image quotient as a function of the parameter p . It is clear that in order to satisfy the 1 to 1 condition, the curve must not have any turning points: that is, it must increase or decrease

monotonically in the appropriate range of p . Mathematically this is expressed as:

$$\left| \frac{df}{dp} \right| > 0 \quad \forall p \in P. \quad (18)$$

Measurement of an image quotient value \bar{i}_0 , corresponding to a parameter value p_0 , is now considered. Associated with acquisition of each image value is an uncertainty due to camera error. It is straightforward to show, using standard error analysis, that the error associated with an image quotient \bar{i} , which has been calculated from the two image values i_1 and i_2 , is given as:

$$\Delta \bar{i} = \Delta i \left(\frac{i_1 + i_2}{i_2^2 - (\Delta i)^2} \right) \quad (19)$$

where Δi is the camera uncertainty. This error has been shown on the ordinate of the graph in Figure 1. If the derivate of f is non-zero in some neighbourhood of p_0 then it is possible to approximate this function linearly. Assuming the error Δi to lie within this neighbourhood, the corresponding error in the parameter value is given as:

$$\Delta p = \Delta \bar{i} / \frac{df}{dp}. \quad (20)$$

Thus, it is possible to obtain a value for the error Δp , associated with parameter recovery, at any point in P -space. An optimisation criterion can then be defined based on some measure of this error. For most applications it will be necessary to minimise the error equally across the whole of P -space. For others it may be that high accuracy parameter recovery is required within a certain range of parameter values. For example, in a medical image application, imaged tissue could be deemed pathological once a characterising parameter changes beyond a threshold level. This would need to be accounted for with some form of weighting in the optimisation criterion. It is interesting to note that in order to minimise Δp , it is necessary to maximise the magnitude of the derivative given in equation (18). This will ensure that any search, carried out to find an optimum f , will tend to move towards regions of search space where the 1 to 1 condition is satisfied.

In theory it is possible to recover the parameter using more than one image quotient. In this case it will be necessary to calculate the error associated with parameter recovery for each of the image quotients and select the one, at each point in P -space, which has

the smallest associated error (Δp). It may be that the optimisation procedure gives a single image quotient which performs better than any other across the whole of P -space. In this situation there is no benefit to using more than one image quotient.

The analysis is now extended to the general problem where the recovery of a K -dimensional parameter vector is required from an \bar{N} dimensional vector of image quotients. Initially the analysis will be restricted to the case where $\bar{N} = K$ and will then be extended to include situations where $\bar{N} > K$. As discussed earlier, if $\bar{N} < K$, then it is not possible to recover K -dimensional data from an \bar{N} dimensional measurement.

The mapping function f , defined as:

$$\bar{i} = f(p) \quad (21)$$

must now be considered a vector valued function of a vector variable. In the following analysis specific results from differential geometry will be used. For further details the reader is directed to for example M. M. Lipschutz, Differential geometry (McGraw-Hill Book Company, New York, 1969). To establish whether the function f provides a 1 to 1 relationship, it is first necessary to consider the behaviour of the determinant of the Jacobian matrix, simply referred to as the Jacobian. This is defined as:

$$\det \left(\frac{\partial f_n}{\partial p_k} \right) = \begin{vmatrix} \frac{\partial f_1}{\partial p_1} & \frac{\partial f_1}{\partial p_2} & \dots & \frac{\partial f_1}{\partial p_k} \\ \dots & \dots & \dots & \dots \\ \frac{\partial f_n}{\partial p_1} & \frac{\partial f_n}{\partial p_2} & \dots & \frac{\partial f_n}{\partial p_k} \end{vmatrix} \quad (22)$$

The Jacobian can be considered the multidimensional equivalent of the one dimensional derivative given in equation (18). The inverse function theorem states that, if the Jacobian is non-zero at a point p_0 in P -space, then there exists a neighbourhood around p_0 where the function f can be approximated linearly as

$$f(p) = f(p_0) + df(p_0)(p - p_0) \quad (23)$$

where df is the differential of f and is given as:

$$df = \frac{\partial f}{\partial p_1} dp_1 + \frac{\partial f}{\partial p_2} dp_2 + \dots + \frac{\partial f}{\partial p_k} dp_k \quad (24)$$

It follows that in this neighbourhood the function f provides a 1 to 1 relationship. Thus, if it is possible to establish that the Jacobian is strictly positive or strictly negative throughout the whole of P -space, the function f will be 1 to 1 everywhere. Once this condition has been established, it is necessary to consider how the error associated with image acquisition maps under f^{-1} , to give the corresponding error in parameter recovery. The error associated with each image quotient is calculated using equation (19). The combination of errors maps out a hypervolume in \bar{I} -space, centred on the point \bar{i}_0 . This has been illustrated in Figure 2 for the case of a 2D P -space, where an ellipse is obtained (or a circle if the errors are equal). An ellipsoid is obtained in 3D space and a hyperellipse in higher dimensions. Although the following analysis will be based on a 2D P -space, the arguments are equally valid in higher dimensions.

The ellipse in \bar{I} -space represents all possible image quotient vectors which could correspond to a camera measurement $\bar{i} = \bar{i}_0$. It is assumed that the region of error lies within the neighbourhood of $\bar{i} = \bar{i}_0$ where the mapping function f can be approximated linearly. Thus, under the mapping f^{-1} , the ellipse in \bar{I} -space maps directly to another ellipse in P -space. This new ellipse is centred on the point $p = p_0$ and represents all possible parameter vectors which could be recovered from the vector of image quotients $\bar{i} = \bar{i}_0$. The error associated with parameter recovery is obtained by considering the worst case scenario: that is the point within the ellipse in P -space which is at the maximum distance from the point $p = p_0$. This maximum distance must be calculated separately for each component, p_k , of the parameter vector to obtain the error associated with recovery of each individual component. To calculate these errors it is necessary to consider how the ellipse is transformed under the mapping f^{-1} , which is linear provided the Jacobian is non-zero.

Under a linear mapping the ellipse will be translated, scaled and rotated. The translation associated with the linear mapping defines the point $p = p_0$ which is mapped to from the point $\bar{i} = \bar{i}_0$. The two other transformations, scaling and rotation, are best understood by considering how a vector $d\bar{i} = d\bar{f}$ in \bar{I} -space, maps under f^{-1} to give a corresponding vector dp in P -space. The vector dp can be calculated from the inverse form of equation (24) which, in matrix form, is given as:

$$d\mathbf{p} = \mathbf{J}^{-1} d\bar{\mathbf{i}} \quad (25)$$

where \mathbf{J} denotes the Jacobian matrix. Note that \mathbf{J}^{-1} exists only if the Jacobian is non-zero. This must be the case if the 1 to 1 condition is to be satisfied.

The vectors \mathbf{A} and \mathbf{B} correspond to the major and minor axes of the ellipse in $\bar{\mathbf{I}}$ -space and are given as:

$$\mathbf{A} = \begin{pmatrix} \Delta \bar{i}_1 \\ 0 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 0 \\ \Delta \bar{i}_2 \end{pmatrix}. \quad (26)$$

Under the mapping \mathbf{f}^{-1} these vectors map to the vectors \mathbf{A}' and \mathbf{B}' which correspond to the major and minor axes of the ellipse in parameter space. Solving equation (25) for each of these vectors gives:

$$\mathbf{A}' = \begin{pmatrix} \Delta p_1^A \\ \Delta p_2^A \end{pmatrix}, \quad \mathbf{B}' = \begin{pmatrix} \Delta p_1^B \\ \Delta p_2^B \end{pmatrix} \quad (27)$$

where Δp_1^A and Δp_2^A are the components of the vector \mathbf{A}' in the direction of p_1 and p_2 respectively. Similarly, Δp_1^B and Δp_2^B are the components of the vector \mathbf{B}' in the direction of p_1 and p_2 respectively. To calculate the error in each component of the parameter vector it is necessary to consider the worst case scenario. It can be seen from Figure 2 that this corresponds to taking the maximum of Δp_1^A and Δp_2^B as the error in p_1 and taking the maximum Δp_2^A and Δp_1^B as the error in p_2 . This error can be specified by a vector $\Delta \mathbf{p}$ and can be calculated for any given point in parameter space. With this measure of the accuracy of parameter recovery across the whole of parameter space, it is possible to define an optimisation criterion. This could simply be based on a sum of the errors at every point in \mathbf{P} -space or could be chosen to favour accuracy of recovery of a subset of the original parameters. Once this optimisation criterion has been defined, a search can be used to find the optimum mapping function \mathbf{f} . It is important to note that, although the above discussion is based on a 2D parameter space, the methodology is equally applicable to any K -dimensional parameter space.

An algorithm for the implementation of the proposed methodology is given as follows:

1. Establish a suitable search space from a parameterisation of mappings b and c .
2. For a given mapping function f calculate the vector of image quotients for each point within a discretised parameter space.
3. For each point, check that the Jacobian is either strictly positive or strictly negative across the whole of parameter space. If this condition is held then compute the inverse of the Jacobian matrix. If not then return to step 1 and define a new mapping function f .
4. Using equation (19), calculate the error associated with image acquisition for each vector of image quotients.
5. From the image quotient vector error calculate the maximum possible error in each component, p_k , of the parameter vector across the whole of parameter space.
6. Use the vector of parameter errors at each point within parameter space to measure the accuracy of parameter recovery.
7. Repeat steps 2-6 with some optimisation technique which enables an optimum mapping function f to be determined.

It is fairly straightforward to extend this methodology to the case in which $\bar{N} > K$: that is, where there are more image quotients than parameter values. Initially every possible K -dimensional subspace of image quotients will need to be defined from the original \bar{N} -dimensional space of image quotients. It will then be necessary to go through the above procedure for each potential subspace and obtain the vector of parameter errors at each point within parameter space. To achieve the maximum possible accuracy the best Δp must be selected at every location within parameter space. Thus every point in P -space will be linked to a specific image quotient combination. It will then be necessary to link every region of the original \bar{N} -dimensional space of image quotients to the particular subspace of image quotients which should be used for parameter recovery. It is important to note that it is necessary to recover the whole parameter vector at each point \bar{i}_0 within a particular K -dimensional subspace of image quotients. It is not possible to attempt to improve the accuracy of the system by recovering different components of the parameter vector from different K -dimensional subspaces of image quotients. This is mathematically invalid.

The mapping function f is a composite function of three separate mappings. Although

the first mapping a , from parameter space to wavelength space, is fixed for a given problem, mappings b and c can vary depending on the choice of optical filters and definition of image quotients. Thus, to define an appropriate search space it is necessary to parameterise mappings b and c . Mapping b , which represents image acquisition, is defined by the positive $N \times M$ matrix R_m^n , given in equation (11). Typically this matrix will contain many elements and an appropriate parameterisation should be based on typical filter response functions. For example, the position of the central wavelength and a measure of width could be used to define a Gaussian shape.

Parameterisation of the mapping function c will be fairly straightforward as there are only a limited number of ways of combining image values to produce independent image quotients. In some applications the form of this mapping may be fixed *a priori*. Thus, it will not increase the overall dimensionality of the search space.

An optimisation method should search the whole space of possible mappings using the optimisation criterion outlined in the previous section. One technique which is ideally suited to this type of search is a genetic algorithm, GA, {see T. Back and H. P. Schwefel, "An overview of evolutionary algorithms for parameter optimisation," *Evolutionary Computation* 1, 1-23 (1993)} as it is straightforward to define a fitness function which measures the accuracy of parameter recovery. Genetic algorithms have been shown to work well on a wide range of problems with objective functions that do not possess "nice" properties such as continuity, differentiability or satisfaction of the Lipschitz Condition {see L. Davis, *The handbook of genetic algorithms* (Van Nostrand Reinhold, New York, 1991), and D. Goldberg, *Genetic algorithms in search, optimization and machine learning* (Addison-Wesley, London, 1989)}.

The above techniques will now be further exemplified by considering their application to the analysis of normal skin composition. Firstly, the prediction of spectral reflectance is considered.

In order to perform mapping a it is necessary to have either a mathematical model which can predict spectral reflectance for a given set of parameter values or some technique for measurement of the appropriate spectrum. For this application we use the

mathematical model developed by Cotton and Claridge {see S. D. Cotton and E. Claridge, "Developing a predictive model of human skin colouring," *Proc. of SPIE Med. Imag.* 2708, 814-825 (1996)}. With this model it is possible to predict the spectral reflectance for a given set of parameters. An outline of the model is now given.

Skin can be considered to be the four-layer structure depicted in Figure 3. A negligible amount of light is reflected from the surface of the skin, thus the surface term in equation (2) can be neglected. Although not absorbing any radiation, the stratum corneum scatters the incoming light in all directions. Light which penetrates this layer can thus be considered diffuse. In the epidermis light is absorbed by the pigment melanin. The absorption at each wavelength can be calculated using the Lambert-Beer law and will depend on the product of the melanin extinction coefficient and the pigment concentration. After passing through the epidermis the light is both scattered and absorbed by the papillary dermis. The absorption results from the presence of blood and scattering from the underlying collagen structure. The simple Kubelka-Munk light theory {P. Kubelka and F. Munk, "Ein Beitrag zur Optik der Farbanstriche", *"Z. Tech. Opt"* 11, 593-611 (1931)} can be used to model the interaction of light with the papillary dermis as the necessary condition of diffuse incident illumination is satisfied. Any light which passes through the papillary dermis into the reticular dermis can be neglected as no significant backscattering occurs in this layer. Using this two-layer light transport model it is possible to obtain the remitted spectra for given concentrations of melanin and blood. A more detailed description of this model can be found in S. D. Cotton and E. Claridge, "Developing a predictive model of human skin colouring", *Proc. of SPIE Med. Imag.* 2708, 814-825 (1996).

For a given papillary dermal thickness, changes in melanin and blood characterise all histological variation and thus define a 2-D parameter space for healthy skin. To carry out the optimisation procedure described above it is necessary to discretise parameter space. This is done at equal intervals to define 10×10 points, each of which corresponds to a spectrum generated by the mathematical model. For simplicity, concentration values will be denoted by a number between 1 and 10. Figures 4a and 4b show how the remitted spectrum changes as melanin and blood are varied respectively. With a change in melanin concentration, the intensity of the whole spectrum is seen to

decrease, with a more pronounced change in the blue region. As the blood concentration is decreased the most significant reduction in intensity is observed in the green region, the resulting shape reflecting the two absorption maxima of oxyhaemoglobin, a blood born pigment.

To define a suitable search space it is necessary to parameterise the mappings b and c . A parameterised form of b is chosen to define a typical interference filter. This is modelled as a square profile with Gaussian decay at each side. Two parameters are required to specify this shape: the central wavelength and a full width half maximum (FWHM). Optimisation is carried out for three such filters, defining a 6-D search space. With three filters giving three image values, i_1 , i_2 and i_3 , the only possible definition of image quotients, if we assume $i_1 = i_3$ is equivalent to $i_3 = i_1$, is given as:

$$\bar{i}_1 = \frac{i_1}{i_3} \quad \bar{i}_2 = \frac{i_2}{i_3} \quad (28)$$

In this instance the mapping c does not increase the dimensionality of the search space.

The optimisation procedure was implemented following the algorithm given above. Initially the vector of image quotients was calculated for every point within the discretised parameter space. This was done using the mathematical model to perform mapping a , the parameterised form of matrix R_n^m to perform mapping b and the equations (28) to perform mapping c . The derivative of each image quotient, with respect to each parameter, was obtained at each point within discretised parameter space using three-point finite difference approximations. The Jacobian matrix was then constructed at every point within parameter space, and providing its determinant was non-zero everywhere, the inverse calculated. If this condition was violated then a new mapping f was defined. The errors associated with image acquisition were then calculated using equation (19). The absolute value of the error in each image value will vary depending on the camera gain setting. Although this constant will not affect the mapping f , it must be estimated in order to calculate the effective camera error. For this application it was taken to be 0.78% of the maximum value of all the image values across parameter space. This corresponds to a camera which has been set to give a maximum reading for the largest spectral reflectance and a camera error of two grey scale levels in an 8-bit representation.

Using the procedure outlined above the error associated with parameter recovery in both melanin and blood was obtained for each point within the discretised parameter space. In order to find an optimum f , it is necessary to minimise the errors in recovery of both melanin and blood across the whole of parameter space. Thus the fitness function for the GA was taken to be the sum of the errors in both melanin and blood. This procedure was implemented in matlabTM using a standard GA to search the space of available mappings.

The boundaries of the search space were chosen such that the central wavelength was constrained to lie in the visible region (400nm-700nm) and such that the widths of the filters were allowed to vary from a FWHM of 25 to 200nm. Although it is now possible to engineer almost any shape of interference filter, this corresponds to an economically viable range of such filters.

Although it was originally assumed that an image quotient defined as i_1 / i_3 would be equivalent to i_3 / i_1 , the results of the GA search showed that this was not the case. The search was initialised for a random seed and, although the same central wavelengths were always obtained, different filters were selected corresponding to i_3 defined in equation (28). Further investigation showed that these local maxima in the search space corresponded to differing distributions of errors both, across parameter space and between the two parameters. This is because the fitness function, or measure of accuracy, was defined as the sum the errors across parameter space for both melanin and blood. Thus, a loss of accuracy in one parameter could be compensated for with an increase in the other. It may be that, with a more exact specification of the error distribution in the fitness function, it would be possible to obtain the same results for every GA search.

Figure 5 shows a filter combination which gave a similar error in the recovery of both melanin and blood. The image quotients were calculated by dividing the filter centred at $\lambda = 473\text{nm}$ and $\lambda = 560\text{nm}$ by the response of the filter centred at $\lambda = 700\text{nm}$. To understand why these specific filters were selected it is necessary to analyse the spectral curves shown in Figure 4. The filters centred at $\lambda = 473\text{nm}$ and $\lambda = 560\text{nm}$

correspond to spectral locations where there is a large change in intensity with the parameters melanin and blood respectively. A third filter was then required in a region of the spectrum in which the remitted light which was either significantly less or significantly more than that of the other two filters. The filter centred at $\lambda = 700\text{nm}$ was chosen as it always gave the largest response at any point within parameter space. This ensured that the derivatives of each image quotient decreased monotonically across the whole of parameter space. The Jacobian, calculated from these derivatives, was strictly positive across the whole of parameter space. It is interesting to note that some alternative filter combinations gave Jacobians which were strictly negative across parameter space, corresponding to alternative local maxima in the search space. If two filters are chosen, to define an image quotient, which vary similarly across parameter space, there will be minimal change in that image quotient and thus it will be of limited value for parameter measurement.

Table 1 and Table 2 give the errors associated with recovery of melanin and blood respectively at every point within the discretised parameter space, for the filter combination given in Figure 5. These errors have been calculated assuming a camera uncertainty of two grey scale levels in an 8-bit representation that is, an error of $(2/255)$. The errors can be seen to increase as both the melanin and blood concentrations increase. This is due to the decrease in the magnitude of the final remitted spectrum as the pigment concentrations increase. Although this absolute error increases, the fractional error at each point actually decreases and it is nearly always possible to differentiate points in parameter space as the error rarely rises above 0.5.

It has been demonstrated that, using an objectively defined set of optical filters, it is possible to recover scene parameters from image data in a way which is insensitive to geometry and incident illumination. In the example problem, discussed above, the error associated with this parameter recovery was found to be relatively small. The invariance of this mapping means that the technique will be particularly applicable to medical image applications where there is significant curvature of the surface of the imaged tissue, such as near a joint. It will also be unnecessary to calibrate the camera to determine the intensity of the incident light. This could help to significantly increase the speed of image acquisition and later processing.

The methodology set out here has been developed for a measurement task, where the scene parameters are known to vary continuously. The technique can also be applied to problems of recognition, where it is necessary to differentiate discrete objects based on some measure of their spectral reflectance. This approach has been discussed in the article G. Healey, "Using colour for geometry-insensitive segmentation," J. Opt. Soc. Am. A 6, 920-937 (1989) who used the idea of normalised colour to identify different regions of normalised colour space corresponding to different metal and dielectric materials. This enabled geometry-insensitive segmentation of an imaged object comprised of a number of different materials.

It will be appreciated that in order to implement the proposed methodology, a look-up table should be established between all possible image quotients and scene parameters. Although this may be time consuming, it is only necessary to carry out this procedure once. Once established, this look-up table will ensure no significant processing after image acquisition, making this technique particularly suitable to real-time applications.

Figure 6 is a flow diagram showing the key steps in the method described above.

It will be appreciated by the person of skill in the art that various modifications may be made to the above described embodiments without departing from the scope of the present invention.

Claims:

1. A method of determining a property or properties of each of a set of filters, which filters are used to select specific wavelength ranges in a system which relies upon a spectral analysis of remitted, emitted, and/or transmitted light to quantify a parameter or parameters of an object or material, the method comprising the steps of:
 - 1) defining a set of potential filter properties
 - 2) defining one or more image quotients, the or each image quotient for a region being obtained by dividing the quantified output of a given filter for that region, the "image value" for that filter, by another image value for that same region;
 - 3) for an object or material to be analysed and for said defined set of potential filter properties and for said given image quotients, obtaining a function mapping points in parameter space to points in image quotient space;
 - 4) determining whether the mapping function provides a 1:1 correspondence between points in parameter space and points in image quotient space; and
 - 5) if the mapping function does not provide a 1:1 correspondence, rejecting said potential filter properties, repeating steps 1) to 4) and, if the mapping function does provide a 1:1 correspondence accepting the potential filter properties as a candidate set of filter properties.
2. A method according to claim 1 and comprising, for a set of potential filter properties accepted as a candidate set of filter properties, determining the accuracy of parameter recovery obtained using said mapping function and determining whether or not the accuracy is sufficient or matches some other criterion.
3. A method according to claim 2, wherein if the accuracy is sufficient or matches said criterion, the candidate filter properties are adopted and if the accuracy is not sufficient or does not match said criterion, steps 1) to 5) are repeated for a different set of filter properties.
4. A method according to claim 2 or 3, wherein the accuracy is determined by:
 - a) calculating the error associated with image acquisition for each vector of each image quotients;

b) from the image quotient vector error, calculating the maximum possible error in each component of the parameter vector across the whole of parameter space; and

c) using the vector of parameter errors at each point within parameter space to measure the accuracy of parameter recovery.

5. A method according to claim 1 or 2 and comprising repeating steps 1) to 5) for a multiplicity of sets of potential filter properties to identify a plurality of candidate filter property sets, determining for each candidate set an error value representing the accuracy of parameter recovery obtained using the corresponding mapping function, and using said candidate set as a basis for determining a preferred set of filter properties.

6. A method according to claim 5 and comprising using a genetic algorithm to determine a preferred set of filter characteristics using said candidate set.

7. A method according to any one of claims 1 to 3 and comprising using a gradient descent algorithm to select an optimal set of filter characteristics, the starting point for the algorithm being a first candidate set of filter properties identified in step 4).

8. A method according to any one of the preceding claims, wherein for each filter the method of the present invention is used to determine the centre wavelength of the filter.

9. A method according to any one of the preceding claims, wherein the method is used to determine the full width half maximum (FWHM) of the filter characteristic.

10. A method according to any one of the preceding claims, wherein step 3) comprises constructing a Jacobian matrix for the mapping function with respect to said parameter(s), and obtaining the determinant of that matrix.

11. A method of analysing body tissue or fluid and comprising using the method of any one of the preceding claims.

12. A method of determining a property or properties of each of a set of filters substantially as hereinbefore described with reference to the accompanying drawings.

13. Apparatus for analysing an object or material having means for conducting a spectral analysis of remitted, emitted, and/or transmitted light to quantify a parameter or parameters of an object or material, the apparatus comprising a plurality of filters for splitting said light into respective components, the filters having properties obtained by using the method of the above first aspect of the invention.

ABSTRACT

Method and Apparatus for Quantifying Material or Object Properties

A method of determining a properties of each of a set of filters, which filters are used to select specific wavelength ranges in a system which relies upon a spectral analysis of remitted light to quantify parameters of an object or material. The method comprises defining one or more image quotients. For an object or material to be analysed and for a given set of potential filter properties, a function mapping points in parameter space to points in image quotient space is obtained. It is then determined whether the mapping function provides a 1:1 correspondence between points in parameter space and points in image quotient space. If the mapping function does not provide a 1:1 correspondence, said potential filter properties are rejected and, steps 2) and 3) repeated. If the mapping function does provide a 1:1 correspondence, the potential filter properties are accepted as a candidate set of filter properties.

Figure 5

RECEIVED
20 OCT 1986
D
11:41 AM

THIS PAGE BLANK (USPTO)

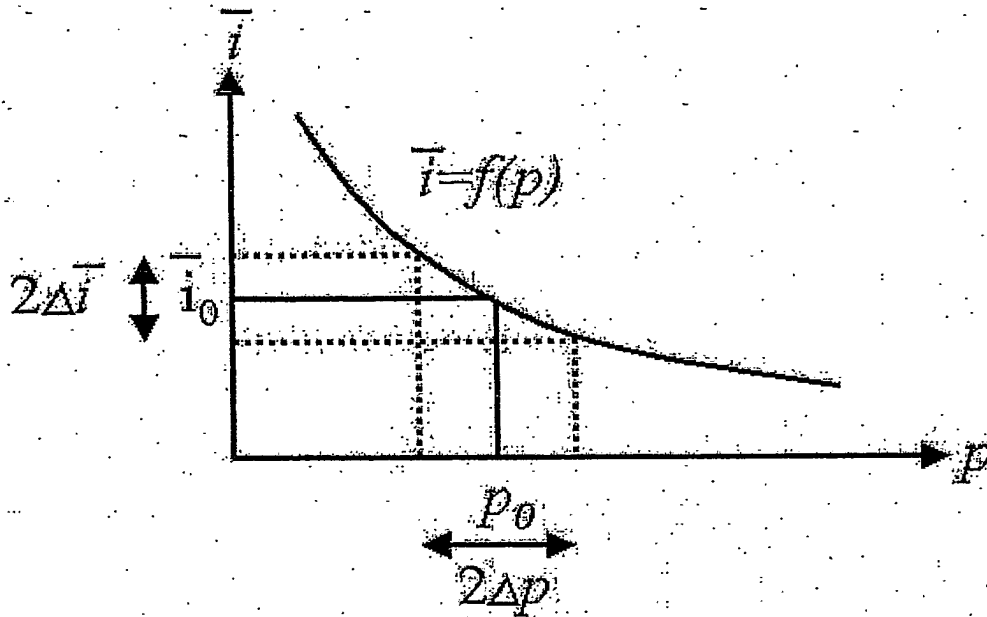


Figure 1

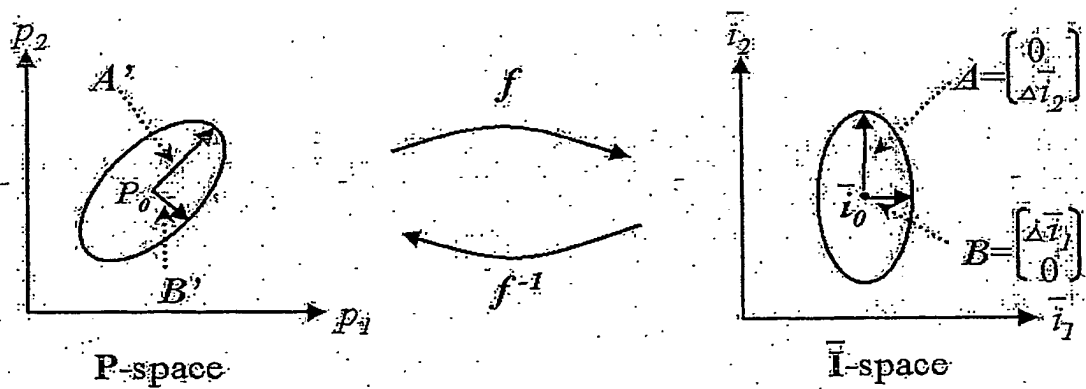


Figure 2

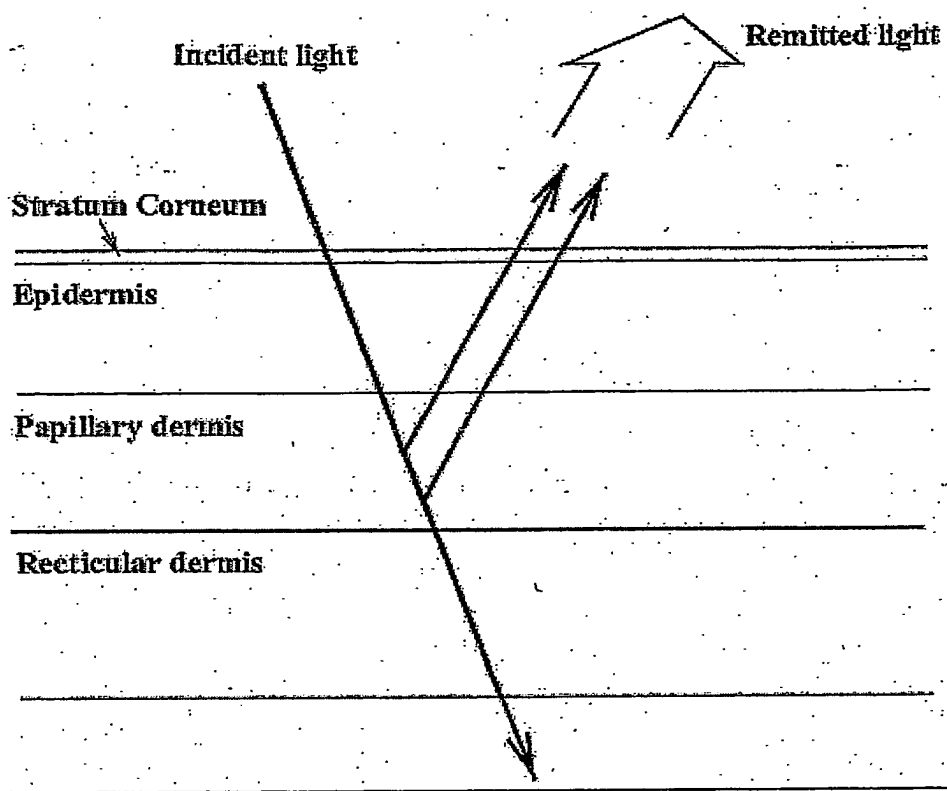


Figure 3

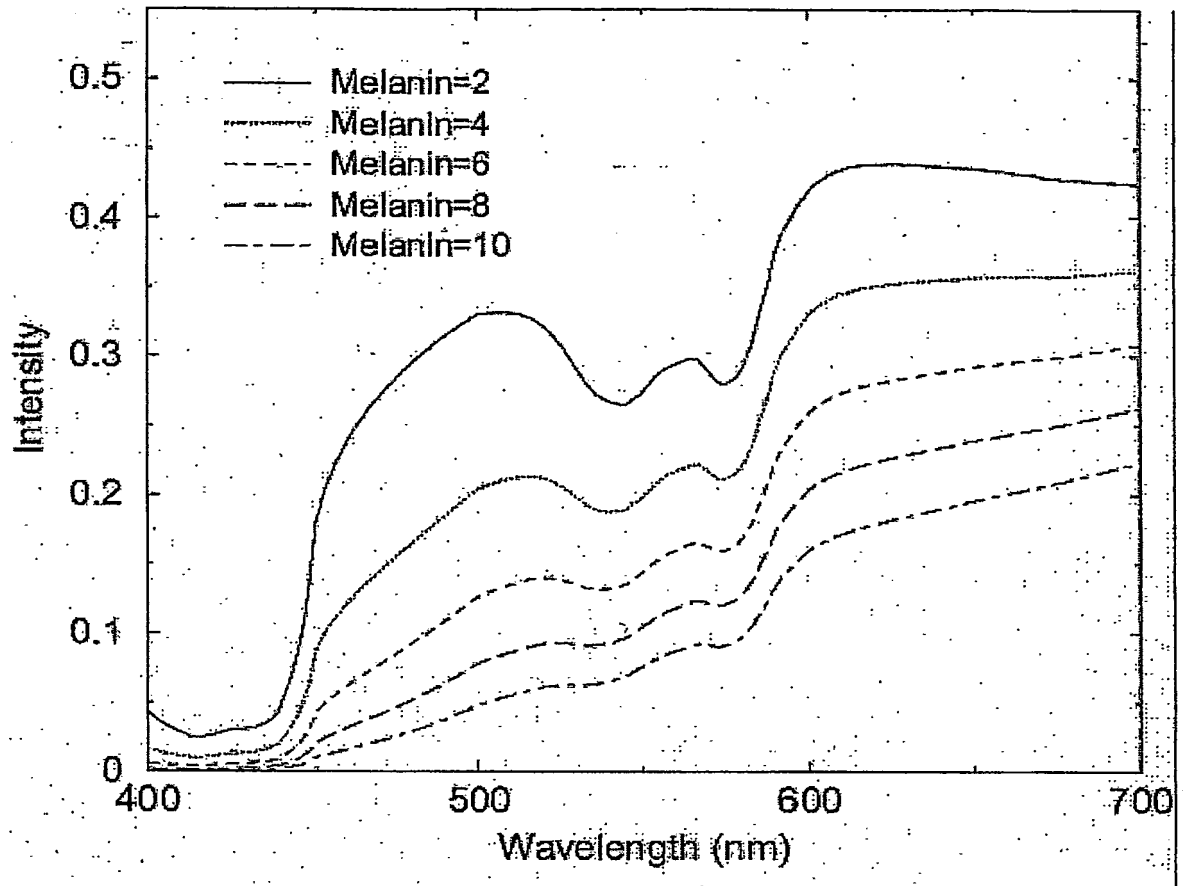


Figure 4a

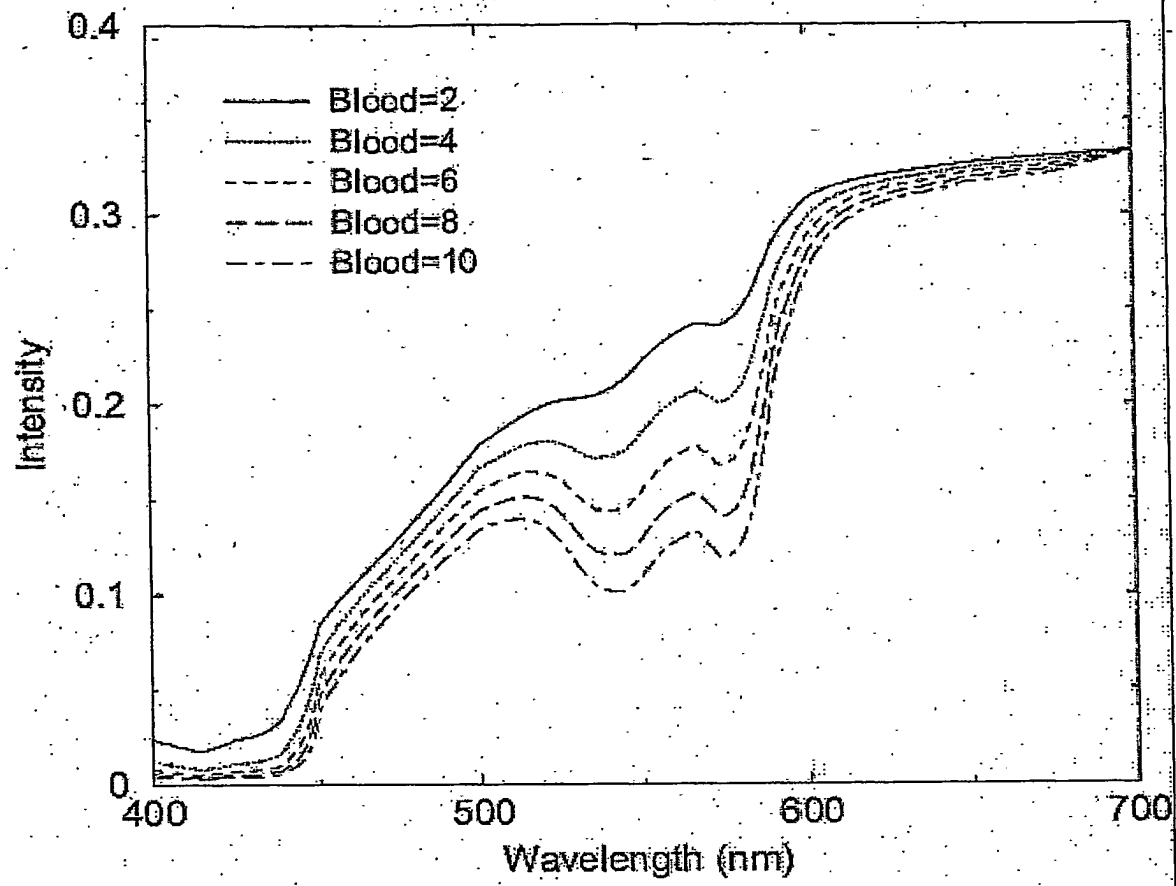
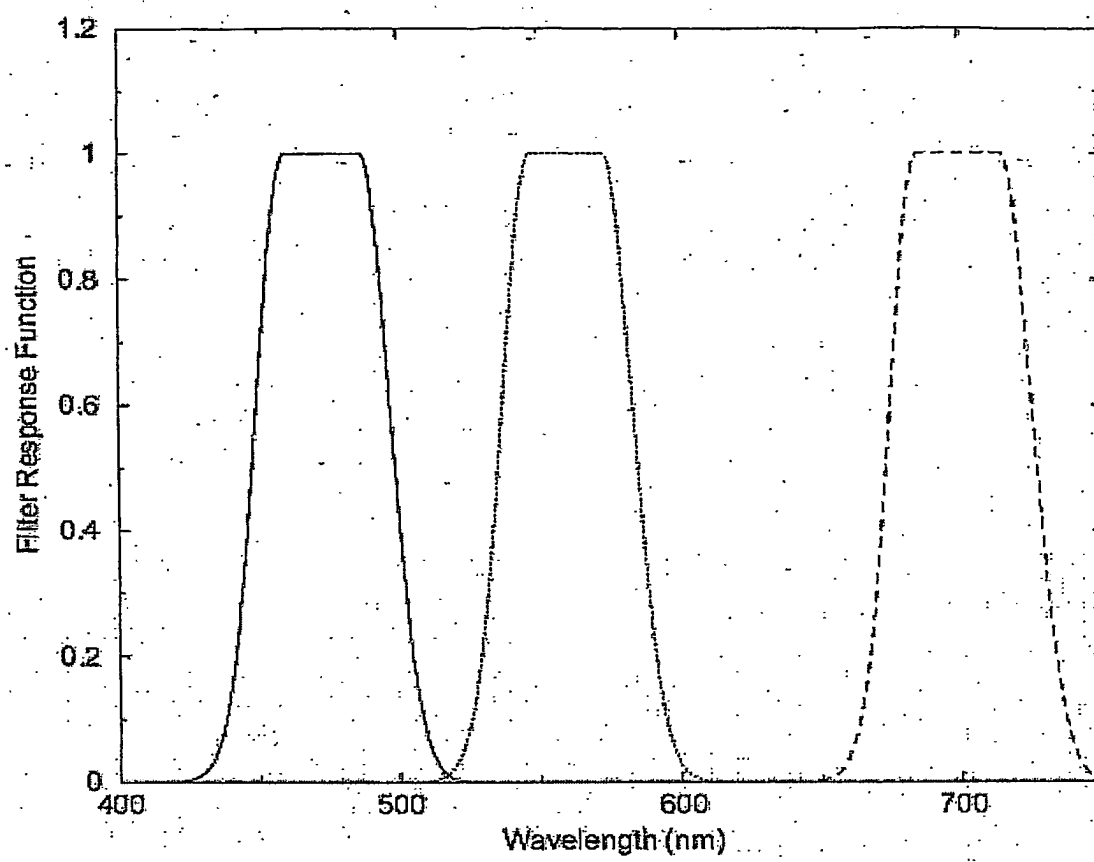


Figure 4b

Figure 5

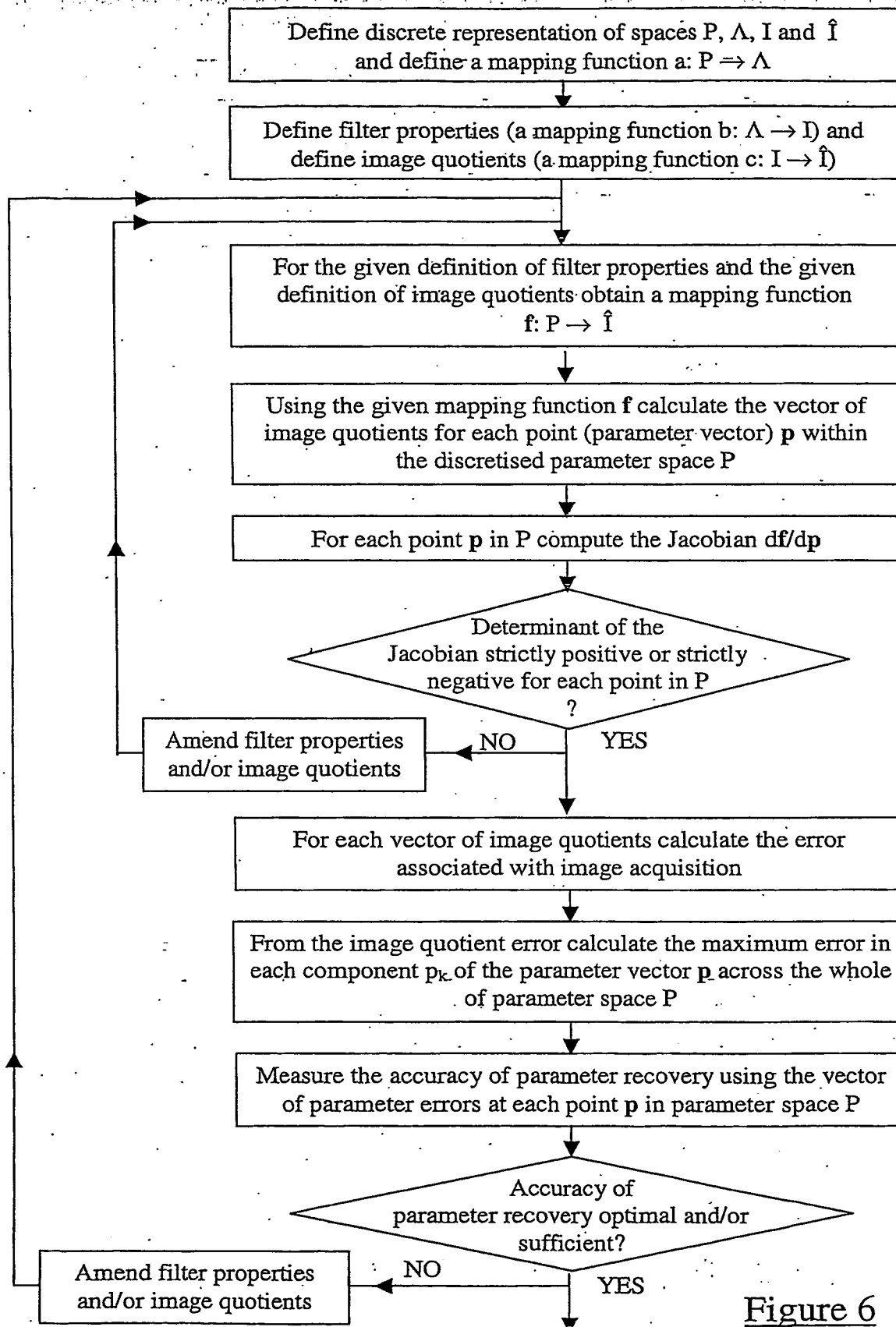


Figure 6

THE PATENT OFFICE
04 SEP 2003
Forwarded to Patents
Interpretation Unit

**This Page is Inserted by IFW Indexing and Scanning
Operations and is not part of the Official Record.**

BEST AVAILABLE IMAGES

Defective images within this document are accurate representations of the original documents submitted by the applicant.

Defects in the images include but are not limited to the items checked:

- ☐ **BLACK BORDERS**
- ☐ **IMAGE CUT OFF AT TOP, BOTTOM OR SIDES**
- ☐ **FADED TEXT OR DRAWING**
- ☐ **BLURRED OR ILLEGIBLE TEXT OR DRAWING**
- ☐ **SKEWED/SLANTED IMAGES**
- ☒ **COLOR OR BLACK AND WHITE PHOTOGRAPHS**
- ☐ **GRAY SCALE DOCUMENTS**
- ☒ **LINES OR MARKS ON ORIGINAL DOCUMENT**
- ☐ **REFERENCE(S) OR EXHIBIT(S) SUBMITTED ARE POOR QUALITY**
- ☐ **OTHER:** _____

IMAGES ARE BEST AVAILABLE COPY.

As rescanning these documents will not correct the image problems checked, please do not report these problems to the IFW Image Problem Mailbox.